MATIBIA UחIVERSITY
OF SCIEПCE AПD TECHחOLOGY

## FACULTY OF MANAGEMENT SCIENCES

DEPARTMENT OF ACCOUNTING, ECONOMICS AND FINANCE

| QUALIFICATION: BACHELOR OF TECHNOLOGY IN ECONOMICS |  |
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| QUALIFICATION CODE: 12BECO | LEVEL: 7 |
| COURSE CODE: AME311S | COURSE NAME: APPLIED MATHEMATICAL <br> ECONOMICS |
| SESSION: JUNE 2019 | PAPER: THEORY |
| DURATION: 3 HOURS | MARKS: 100 |


| FIRST OPPORTUNITY EXAMINATION QUESTION PAPER |  |
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| EXAMINER(S) |  |
|  | MR EDEN TATE SHIPANGA |
| MODERATOR: | PROF T. SUNDE |

## INSTRUCTIONS

1. Answer ALL the questions.
2. Write clearly and neatly.
3. Number the answers clearly.

## PERMISSIBLE MATERIALS

1. PEN,
2. PENCIL
3. CALCULATOR

THIS QUESTION PAPER CONSISTS OF 2 PAGES (Including this front page)

## Question 1 [25 Marks]

Given $\mathrm{Y}=\mathrm{C}+\mathrm{I}_{0}+\mathrm{G}_{0}$,
$\mathrm{C}=\alpha+\delta \mathrm{Yd} \quad(\alpha>0 ; 0<\delta<1)$
$\mathrm{T}=\gamma+\beta \mathrm{Y} \quad(\gamma>0 ; 0<\beta<1)$
Where $\gamma$ is non-income tax, $\beta$ is income tax, $\delta$ is marginal propensity to consume, $\alpha$ is fixed constant, Y (national income), $\mathrm{I}_{0}$ (investment) and $\mathrm{G}_{0}$ (government expenditure)

1. Find the reduced form of equilibrium income $\left(\mathrm{Y}_{\mathrm{e}}\right)$.

5 marks
2. Do comparative static to find the effect of government spending, non-income tax and income tax on equilibrium income.

15 marks
3. If $\alpha=85 ; \delta=0.75 ; \gamma=20 ; \beta=0.2 ; \mathrm{I}_{0}=45 ; \mathrm{G}_{0}=50$, find the effects of lump sum tax increase by $\$ 1$ billion?

5 marks

## Question 2 [25 Marks]

1. Solve the following system of equation using Cramer's rule

$$
\begin{aligned}
& 8 X_{1}-X_{2}=16 \\
& 2 X_{2}+5 X_{3}=5 \\
& 2 X_{1}-3 X_{3}=7
\end{aligned}
$$

10 marks
2. Optimise the following function, using a) Cramer's rule for the first order condition and b) the Hessian for the second-order condition:

$$
y=x_{1}^{2}-7 x_{1}-x_{1} x_{2}+2 x_{2}^{2}-2 x_{2}+2 x_{2} x_{3}+2 x_{3}^{2}+x_{3}-3 x_{1} x_{3}
$$

15 marks

## Question 3 [25 Marks]

Give the input matrix and the final demand vector

$$
A=\left[\begin{array}{ccc}
0.05 & 0.25 & 0.34 \\
0.33 & 0.10 & 0.12 \\
0.19 & 0.38 & 0
\end{array}\right] \quad d=\left[\begin{array}{c}
1800 \\
200 \\
900
\end{array}\right]
$$

(a) Explain the economic meaning of the elements $0.33,0$ and 200
(b) Explain the economic meaning (if any) of the third column sum
(c) Explain the economic meaning (if any) of the third row sum
(d) Find the solution output levels by Cramer's rule

## Question 4 [25 Marks]

Consider the following national income model (tax ignored).

$$
\begin{aligned}
& Y-C(Y)-I(i)-G_{0}=0 \\
& k Y+L(i)-M_{s 0}=0 \\
&\left.\hline 0<C^{\prime}<1 ; I^{\prime}<0\right] \\
& {\left[k>0 ; L^{\prime}<0\right] }
\end{aligned}
$$

Analyse the comparative statics of the model to find the effect of expansionary fiscal and monetary policies?

